

1 Probability of Identification (POI): a Statistical Model for the Validation of Qualitative Botanical
2 Identification Methods

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13
14 **Abstract**

15
16 A qualitative botanical identification method (BIM) is an analytical procedure which returns a
17 binary result (1 = Identified, 0 = Not Identified). A BIM may be used by a buyer, manufacturer
18 or regulator to determine whether a botanical material being tested is the same as the target
19 (desired) material or whether it contains excessive non-target (undesirable) material. We
20 describe the development and validation of studies for a BIM based on the idea of a proportion
21 of replicates identified, or probability of identification (POI), as the basic observed statistic. The
22 statistical procedures proposed for data analysis follow closely those of the probability of
23 detection (POD), and harmonize the statistical concepts and parameters between quantitative and
24 qualitative method validation. Use of POI statistics also harmonizes statistical concepts for
25 botanical, microbiological, toxin and other analyte identification methods that produce binary
26 results. The POI statistical model provides a tool for graphical representation of response curves
27 for qualitative methods, reporting of descriptive statistics, and application of performance
28 requirements. Single collaborator and multi-collaborative study examples are given.
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44 **1. Introduction**

45
46 A “Botanical” is an herbal type of dietary supplement regulated in the USA under the Federal
47 Food, Drug, and Cosmetic Act of 1938, as amended by the Dietary Supplement Health and
48 Education Act of 1994 (1). More recently Current Good Manufacturing Practices (cGMPs) for
49 foods and dietary supplements (2) issued by FDA has tasked manufacturers with authentication
50 of all botanical ingredients. As a consequence, both processors of botanicals and regulators are
51 interested in the verification of the identity of botanical materials. Thus, the development of
52 reliable methods for the identification of botanical materials and minimum acceptable levels of
53 contamination are critical.

54
55 A botanical identification method (BIM) is any qualitative method which reliably identifies a
56 botanical material and returns a binary result of either 1 = “identified” or 0 = “not identified”.
57 The actual method used can be presumed unknown and a “black box” with respect to the
58 protocols involved in the validation studies. The BIM must be validated in terms of inclusivity,
59 exclusivity, probability of identification, robustness, reproducibility, repeatability, and other
60 criteria.

61
62 The heart of the BIM is the probability of Identification (POI) model. The POI model has been
63 developed as a means of characterizing and validating the performance of a qualitative method
64 based on simple statistics and associated confidence intervals (3,4). Figure 1 (modified from
65 Wehling, 2011) shows a plot where the concentration of the target material increases towards the
66 right while the concentration of a non-target material increases to the left. The parameter of
67 interest is the POI (the vertical axis), which is defined as the probability, at a given percentage of
68 target material, of getting a positive response by the detection method. The positive response of
69 the BIM indicates that the test material matches the target botanical material. While the plot in
70 Figure 1 is symmetric, POI plots are usually asymmetric. The POI model is based on the
71 probability of detection (POD) model which was developed for binary qualitative methods for
72 detection of biological threat agents (3,4).

73
74 The POI, as illustrated in Figure 1, is dependent on the concentration of the target botanical
75 material. The probability of a positive response increases as the concentration of the target
76 botanical increases and decreases as the concentration of the non-target material increases. The
77 goal of method development and validation is to first determine if the method meets standard
78 method performance requirements (SMPRs), and secondly to characterize how the method
79 makes the transition from a negative to a positive response.

80
81 The SMPRs will specify the target botanical materials (inclusivity sampling frame), the non-
82 target materials (exclusivity sampling frame), the physical form of the materials, the minimum
83 concentration of target material that is acceptable in the presence of non-target material and the
84 maximum concentration target material that is unacceptable. These latter materials are the
85 specific superior and specific inferior test materials (SSTM and SITM, respectively). The
86 idealized goal of the BIM is to discriminate (with a specified degree of confidence, e.g., 95%)
87 between the SSTM (for which the POI is high) and the SITM (for which the POI is low).
88 Additionally, samples of the SSTM and SITM may be mixed to obtain the intermediate test
89 concentrations that are used to characterize the POI curve in its transitional range.

90
91 In some studies, full characterization of the transition of the POI curve may be of lesser
92 importance and the intermediate concentrations omitted. In this case the only concentrations
93 used are those for which the performance requirements are applied, typically the SITM and
94 SSTM (0% and 100% SSTM, respectively).
95
96 Two factors are important to method development: industrial-regulatory requirements and the
97 technological limit (“state of the measurement art”). If the technological limit exceeds the
98 industry-regulatory requirement, then the industrial-regulatory requirement can be set at a value
99 reasonably attainable by existing technology. In this case, the cost of the analysis may be the
100 major factor governing validation study design. If the technological limit cannot meet the
101 industrial-regulatory requirement, then improved technology must be developed before a BIM fit
102 for the purpose intended can be found.

103 **2. Glossary**

104
105
106 Analytical Parameter (AP): A measured or computed analytical value used to determine whether
107 the test material matches the target material. The analytical parameter may be based on
108 morphological features, genetic sequences, chromatographic patterns, spectral patterns, or
109 any other metric appropriate for the target material.
110

111 Botanical: Of, or relating to, plants or botany. May also include algae and fungi. May refer to
112 the whole plant, a part of the plant (e.g. bark, woods, leaves, stems, roots, rhizomes,
113 flowers, fruits, seeds, extracts, etc.), or an extract of the plant.
114

115 Botanical Identification Method (BIM): A method that establishes identity specifications for a
116 botanical material and allows determination, within a specified statistical limit, that a test
117 material is a true example of the target botanical material and meets the identity
118 specifications. Thus, a method answers the question, “*Is the test material the same as the*
119 *target material?*” not “*What is this material?*” In most cases, the method will be
120 validated to achieve this goal by comparison of the test material with materials from the
121 inclusivity panel and will return a yes/no (or, in some cases, a consistent/non-consistent)
122 answer.
123

124 Candidate Method: The method to be validated.
125

126 Exclusivity: Ability of a BIM to correctly reject non-target botanical materials.
127

128 Exclusivity Sampling Frame (ESF): A list of practically obtainable non-target botanical
129 materials that have similar taxonomic, physical, or chemical composition characteristics
130 that are expected to give a negative result when tested by the BIM.
131

132 Exclusivity Panel: A subset of the exclusivity sampling frame that is selected for the validation
133 study. These materials should be authenticated by an appropriate method.
134

135 False Negative Fraction (FNF): $1 - \text{POI}$ for 100% SSTM. Not defined for other concentrations.

136
137 False Positive Fraction (FPF): POI for 100% SITM. Not defined for other concentrations.
138
139 Identity Specification: The morphological, genetic, chemical, or other characteristics that define
140 a target botanical material. Specifications may include, but are not limited to, data from
141 macroscopic, microscopic, genetic (e.g. DNA sequencing, barcoding), chromatographic
142 fingerprinting (e.g. CE, GC, LC, TLC), and spectral fingerprinting methods (e.g. IR, NIR,
143 NMR, MS, UV/VIS) methods.
144
145 Inclusivity: Ability of a BIM to correctly identify variants of the target material that meet the
146 identity specification.
147
148 Inclusivity Sampling Frame (ISF): A list of practically obtainable botanical materials that are
149 expected to give a positive result when tested by the BIM. The inclusivity sampling
150 frame should be sufficiently large that the botanical variation is adequately represented.
151 Sources of variation may include, but are not limited to, species, sub-species, cultivar,
152 growing location, growing conditions, growing season, and post-harvest processing.
153
154 Inclusivity Panel: A subset of the inclusivity sampling frame that is selected for the validation
155 study. These materials should be authenticated by an appropriate method.
156
157 Laboratory Sample: Sample as prepared for sending to the laboratory intended for inspection or
158 testing.
159
160 Non-Target Botanical Material: Any botanical material that does not meet the identity
161 specification.
162
163 Physical Form: Botanical materials exist in a number of physical forms. The form(s) to be
164 analyzed by the method will be specified by the SMPRs.
165
166 Probability of Identification (POI): The expected or the observed fraction of test portions that
167 provide a positive result at a given concentration when tested by the BIM.
168
169 Sample: A small quantity, taken from a population or lot that is a representative selection of the
170 whole.
171
172 Specified Inferior Test Material (SITM): A mixture of botanical materials that contains the
173 maximum concentration of target material that is considered unacceptable, as specified
174 by the SMPRs. The BIM must reject this material with a specified minimum level of $(1 -$
175 $POI)$ with 95% confidence. The ideal BIM would reject the SITM 100% of the time (i.e.,
176 identify 0% of the time). The SITM will typically be high quality target material mixed
177 with the worst-case (for identification) non-target material.
178
179 Specified Superior Test Material (SSTM). A mixture of botanical material that contains the
180 minimum acceptable concentration of the target material, as specified by the SMPR. The
181 BIM must identify this material with a specified minimum level of POI with 95%

182 confidence. The ideal BIM would identify the SSTM 100% of the time. The SSTM will
183 typically be high quality target material mixed with a small amount of worst-case (for
184 identification) non-target material.

185
186 Standard Method Performance Requirements (SMPRs): Performance requirements based on the
187 fitness for purpose statement for each method. For BIMs, the SMPRs should minimally
188 include the physical form of the sample, the ISF, the ESF, the SSTM, and the SITM.

189
190 Target Botanical Material: The botanical material of interest as described in the identity
191 specification.

192
193 Target Material Concentration: The percentage, by weight, of the target botanical material in the
194 sample.

195
196 Test Portion: The portion of the laboratory sample that is subjected to analysis by the method.

197 198 **3. Inclusivity Panel**

199
200 When a botanical material is identified for development of a BIM, a target material is usually
201 specified. Biological materials, however, are complex. While the genotype of a species or sub-
202 species may be relatively stable, the phenotype (metabolite composition) will vary with location,
203 season, weather, and many other variables. Thus, “target material” becomes “target materials”.
204 Ideally, the target materials will encompass the expected botanical variation.

205
206 An inclusive list of all the variations for a target material can be quite extensive and impractical.
207 For example, the list for a specific botanical might ideally include samples from the last 10 years
208 from 8 international locations (80 samples). In reality, only 25 of the desired samples may be
209 practically obtainable. These 25 obtainable samples comprise the inclusivity sampling frame
210 (ISF). Of these 25 samples, only 10 may be selected for method development/validation. These
211 10 samples comprise the inclusivity panel.

212
213 For each candidate BIM, the SMPRs must provide a list of all necessary botanical variants that
214 should provide a positive identification. This should include species, varieties, geographic or
215 seasonal variants, and other variants that are believed to possibly associate with BIM
216 identification performance. The information tabulated should include variety, season, locality,
217 source from which the variant is obtainable, species, variety or subclass, and whether or not it is
218 essential the variant be tested. Age of the plant may be a factor of importance. The subset of this
219 list which is practically obtainable for a validation study is the ISF.

220
221 The SMPRs should identify the minimum number of materials in the ISF that must be tested to
222 verify identifiability (inclusivity panel), as well as the number of replicates needed. If at all
223 possible, any exchangeability (choice among variants which SMPRs do not discriminate) should
224 result in random selection from the ISF.

225
226 Generally, the inclusivity panel of target variants should include all of the ISF if the number of
227 variants is small. Otherwise all necessary variants plus additional ones randomly selected should

228 comprise the inclusivity panel. More randomized replicate variants may allow a quantitative
229 statistical inference to be made concerning inclusivity. An inclusivity panel with no
230 randomization, only subjective selection, does not permit statistical statements of inference with
231 respect to inclusivity.

232

233 **4. Exclusivity Panel**

234

235 The list of non-target materials can be quite extensive, theoretically including all the botanicals
236 not on the inclusivity list. However, of prime interest are those materials that might accidentally
237 or intentionally be used to replace or augment the target materials. The exclusivity list should
238 include botanical materials that are closely related taxonomically, morphologically, or
239 phenotypically. Again, this list may be extensive and impractical. The exclusivity sampling
240 frame (ESF) will be comprised of those botanical materials that are practically obtainable. The
241 exclusivity panel will comprise those samples used for method development and validation.

242

243 The SMPRs must provide a list of all necessary or commonly encountered non-target botanical
244 materials and variants. This list should include botanical materials that are believed to
245 accidentally or intentionally alter the composition of the target material. The information
246 tabulated should include variety, season, locality, source from which the variant is obtainable,
247 species, variety or subclass, and whether or not it is essential the non-target material be tested.
248 The subset of this list which is practically obtainable for a validation study should then be
249 identified as the ESF.

250

251 The SMPRs should identify the minimum number of non-target materials of the ESF that should
252 be included on the exclusivity panel and be tested to verify non-identifiability, as well as the
253 number of replicates needed. If at all possible, any exchangeability (choice among variants
254 which expertise does not discriminate) should result in random selection from the ESF.

255

256 Generally, the exclusivity panel of authentic variants should include all of the ESF if the number
257 of variants is small. Otherwise all necessary variants plus optional ones randomly selected to
258 comprise a set as specified by the ERP. More replicates and randomization may allow a
259 quantitative statistical inference to be made concerning exclusivity.

260

261 **5. Inclusivity and Exclusivity Testing**

262

263 The purpose of inclusivity/exclusivity testing is to verify that the BIM correctly identifies all of
264 the botanical materials listed in the ISF and correctly rejects all non-target materials listed in the
265 ESF. The BIM should clearly and unequivocally discriminate between the target and non-target
266 materials. Testing materials from the inclusivity/exclusivity panels should provide sufficient
267 confidence that this is the case. The number of samples tested and the number of replicates is
268 specified by the SMPRs.

269

270 Typically, inclusivity/exclusivity panel results are verified during method development. Any
271 unexpected results should be followed up with a minimum number of additional replications
272 (determined by the SMPRs) to characterize the POI on the variant quantitatively. If the variant
273 fails to meet minimum acceptable performance requirements as set by the SMPRs, the exception

274 should be noted in the study report and reviewed for acceptability by the relevant method
275 reviewers.

276
277 If the method development results are acceptable, inclusivity and exclusivity should be verified
278 in an independent laboratory, although possibly on a less intensive (fewer replicates or randomly
279 selected variants) basis, as the objective is verification, not validation. If no randomization is
280 used, all that can be reported is the actual results obtained, but without suggestive quantitative
281 statistics. For example, without randomization, the use of percentages or other quantitative
282 measures is inappropriate.

283 284 **6. Performance Requirements and the Specification and Preparation of the SITM and** 285 **SSTM**

286
287 After inclusivity and exclusivity studies have been completed, target and non-target material(s)
288 are chosen to verify that the method can discriminate between the SSTM and the SITM. Either
289 the worst-case non-target materials or perhaps the most common non-target materials would
290 typically be chosen. In addition, a combination of target and non-target materials should be
291 selected to challenge method performance (worst-case, most common, etc.). The number of
292 samples tested and the number of replicates is specified by the SMPRs.

293
294 The SMPRs should identify the composition and the minimum POI acceptable (with 95%
295 confidence) for the SSTM and SITM. The SSTM and SITM would be made of the target
296 material(s) mixed with the combination of non-target material(s).

297 298 **7. Application of the POI to an Analytical Method**

299
300 Analytically, a BIM will be based on a series of measured values. These values may be derived
301 from morphological features, genetic sequences, chromatographic patterns, spectral patterns, or
302 any other metric appropriate for the target material. These values will be combined to provide a
303 single univariate analytical parameter (AP) that will be used to determine whether the test sample
304 matches or does not match the materials from the inclusivity panel. This decision is made by
305 comparing the AP of the test material to a threshold value that is usually based on the
306 characterization of the POI as a function of target material concentration.

307
308 The first step in the development of the method is the selection of the analytical approach and the
309 analysis of samples from the ISF and ESF. Multiple replicates of multiple samples should,
310 ideally, give results similar to those in Figure 2. Here, the AP, not the POI, is plotted on the
311 vertical axis. The standard deviations are shown as sample distribution functions rather than as
312 error bars. Ideally, the separation of the ISF and ESF samples should be as large as possible.
313 For the data in Figure 2, the threshold to distinguish between the ISF and ESF can be placed at
314 almost any value of the AP.

315
316 The width of the sample distribution function will depend on the number of samples analyzed
317 from the ISF and ESF. If replicates of a single sample are analyzed, then the width of the
318 distribution will be narrow (a smaller standard deviation) and only reflect the instrumental

319 variance. As more samples are analyzed from the ISF and ESF, the distribution functions will
320 broaden reflecting the increasing biological variance.

321
322 The next step is to determine whether the method can distinguish between the SSTM and the
323 SITM. The concentrations of the SSTM and the SITM are specified by the SMPRs. Figure 2
324 illustrates an arbitrary specification. It can be seen that the distributions of the SSTM and SITM
325 are completely resolved and the threshold must be located exactly between the two distributions
326 to provide 100% identification of the SSTM (POI=1) and 100% rejection of the SITM (POI=0),
327 If the concentration of target material in the SSTM was lower or the concentration in the SITM
328 was higher, the distribution functions would overlap and 100% identification or rejection would
329 not be possible. In this case, the confidence limit would have to be lowered or another method
330 selected.

331
332 Finally, the shape of the POI curve can be determined. As shown in Figure 3, concentrations of
333 the target materials must be prepared that fall between the SSTM and SITM. In each case, the
334 threshold will intersect each peak and determine the POI. As the SSTM:SITM values change
335 from 1:0 to 3:1 to 1;1 to 1;3 to 0:1, the POI decreases from 1.0 to 0.9 to 0.5 to 0.1 to 0.0.

336
337 The models in Figures 2 and 3 assume that the SITM and SSTM have the same, symmetrical
338 distribution function and width. This is not a reasonable assumption for real samples. However,
339 the POI model is valid regardless the shape of the distribution functions involved.

340

341 **8. A Specific Example – American ginseng mixed with Chinese ginseng**

342

343 A data set is presented here that illustrates the analytical measurements discussed in the previous
344 section. The target botanical material is American ginseng and the non-target material is
345 Chinese ginseng. The inclusivity panel consists of 43 American ginseng (AG) samples grown in
346 the US (harvested over 3 years from 20 different farms in Wisconsin) and the exclusivity panel
347 consists of 8 Chinese ginseng (CG) samples grown in China (Table 1).

348

349 The AG and CG samples were analyzed by direct injection mass spectrometry and yielded
350 spectra with approximately 1000 ions. The SSTM and SITM were generated synthetically by
351 combining different percentages of the AG and CG mass spectra. For example, the spectra for
352 98% AG mixed with 2% CG was computed as 0.98 of an AG spectra added to 0.02 of a CG
353 spectra. In all, 344 SSTM spectra were generated (43 AG x 8 CG).

354

355 The multivariate data (1000 variables) were analyzed using SIMCA (soft independent modeling
356 of class analogy) (Appendix A). SIMCA produced a single univariate value, the Q residual, that
357 was used to compare the test (100% CG, SSTM, and SITM) and the target (100% AG) materials.
358 In every case, the SIMCA model was based on 100% AG and a single principal component. The
359 Q residual, describes how far a sample falls outside the model (Appendix A).

360

361 Figure 4A shows the inclusivity/exclusivity study. The Q residual is plotted for individual
362 samples. With 100% AG (inclusivity panel samples) as the model, it can be seen that the CG
363 (exclusivity panel samples) falls well above the 95% confidence limit (dashed line). Both the
364 AG and CG show considerable variation on the vertical axis that reflects the biological variation.

365 Two of the AG samples fall above the 95% confidence limit, which is 4.6% for 43 samples and
366 is to be expected.

367
368 For the SSTM/SITM study, 98% and 90% AG were arbitrarily selected as the SMPRs for this
369 model. Figure 4B shows the SSTM samples (98% AG) as well as 100% AG and 100% CG
370 samples. The pattern of 8 groupings for the SSTM samples reflects that all 43 AG samples were
371 diluted by each of the 8 CG samples in sequence. A threshold of a Q residual value of 9.0 was
372 selected arbitrarily and provides 99.4% positive identification (342 out of 344).

373
374 Figure 4C shows the SITM at 90% AG. The threshold provides negative identification of the
375 SITM for 99.1% of the samples (341 out of 344). The distribution of the SSTM and SITM are
376 plotted in Figure 5A. The distributions appear to be roughly symmetrical. However, since the
377 vertical axis is a logarithmic scale, the distributions are badly skewed on a linear scale and have
378 dramatically different widths. It can be seen that if the SSTM were specified at a lower
379 concentration of AG or the SITM at a higher concentration of AG, the method would not be
380 appropriate unless lower confidence limits were chosen.

381
382 Based on the AP threshold shown in Figures 4B, 4C, and 5, the POI in Figure 5B was computed.
383 Synthetic samples of 96%, 94%, and 92% were generated and analyzed. The curve shape for the
384 POI is very non-symmetric.

385
386 For our example, the SSTM corresponds to 98% AG mixed with 2% CG. The required
387 minimum POI is 0.90 with 95% confidence for 100% SSTM (Table 2). The SITM corresponds
388 to 90% AG mixed with 10% CG. The required maximum POI is 0.10 with 95% confidence.
389 Table 2 shows that, for these performance requirements, 60 replicates must be tested at each
390 level with no more than 2 failures. More stringent requirements (i.e., 0.95 and 0.05 with 95%
391 confidence would require more replicates and/or fewer failures. Conversely, less stringent
392 requirements would require fewer replicates. Depending upon the desired performance
393 requirement for SSTM or SITM, alternative test plans may be selected from Table 3. For more
394 plans, see LaBudde (7).

395 396 **9. Single Laboratory Validation**

397
398 Consider an example of a BIM being evaluated with respect to the performance requirements of
399 Table 2. The internal operating methodology of the BIM is possibly a trade-secret of the method
400 developer, so may not be known at the time of validation. All that is known for sure is that a test
401 portion is utilized by the method, and binary result of 1= Identified or 0 = Not Identified is
402 returned. If there are no SMPRs, the method would be “characterized” as opposed to
403 “validated”.

404
405 Consider testing in a single independent laboratory, or a “single laboratory validation” (SLV).
406 With respect to the performance requirements of Table 2, the SITM and SSTM were used to
407 prepare mixtures in the proportions 0%:100%, 33%:67%, 67%:33% and 100%:0%. From each
408 of these mixtures, 60 test portions are prepared, randomized and labeled in a masked way. The
409 test portions are measured by the BIM, each with a result of 0 or 1. Suppose example results are
410 as shown in Table 4. Note the false positive fraction (FPF) performance requirement succeeds at

411 0% SSTM, because no more than 2 test portions reported identification. Also, the false negative
412 fraction (FNF) performance requirement at 100% SSTM succeeds because, in both cases, fewer
413 than 2 test portions were not identified.

414
415 Using the methods of Wehling(3) and LaBudde(5,6), the reported 1-sided and 2-sided 95%
416 confidence intervals on the POI would be as shown in Table 5. Note that the 1-sided 95%
417 confidence limit for the POI falls below 10% at 0% SSTM and above 90% at 100% SSTM,
418 indicating performance requirement success. The results in Table 5 are plotted in Figure 6.

419
420 Because the concentrations (viz., % SSTM) are known with certainty here, one of several
421 regression models might be fit to possibly (although this is not guaranteed) obtain more precise
422 estimates of POI and its confidence limits, but at the expense of some additional assumptions
423 (see Appendix B).

424

425 **10. Collaborative Study**

426

427 The primary purpose of a collaborative study is to establish that performance is reproducible
428 among different collaborators (laboratories). A secondary purpose might be to compare the
429 candidate method to another (possibly “gold standard”) method to establish differential
430 performance (e.g., equivalency) across laboratories.

431

432 The primary purpose requires a minimum number of collaborators whose data persist (i.e., not
433 excluded for cause) until the final results of the study. Rules of thumb in statistical mixed
434 modeling (treating the collaborator effect as random) suggest that fewer than 6 collaborators
435 does not allow inference with respect to the general collaborator population, 8 collaborators
436 allows reasonable estimation, and 10 collaborators is desirable. More than 10 collaborators is
437 useful, but not necessary. For fewer than 6 collaborators, the collaborator effect should be
438 regarded as fixed, and any inferences are applicable only to that particular set of collaborators,
439 not some hypothetical general population of collaborators. The recommendation is therefore that
440 12 or more collaborators should be enrolled in the study, with a desired 8 to 10 remaining after
441 removal for cause, and an absolute limit of no less than 6 remaining until the study end. Studies
442 with this minimum number of collaborators can hope to provide a measure of collaborator effect
443 or collaborator-method interaction, if one of reasonably large size exists.

444

445 Concentration levels (i.e., percentage of SSTM in a SSTM:SITM mix) must include 0% SSTM
446 (100% SITM) and 100% SSTM (0% SITM) in order to establish performance requirements
447 (Figure 2). In addition, it is sometimes beneficial to provide for two intermediate concentrations
448 (e.g., 33% and 67%) in order to provide information about identification performance across the
449 range where the POI changes.

450

451 In order to isolate a collaborator effect in the presence of quantal noise (repeatability error), 12
452 replicates per collaborator is the suggested minimum necessary. Therefore the smallest
453 acceptable collaborative study final data would be 6 collaborators x 12 replicates = 72 test
454 portions.

455

456 It should be noted that a performance requirement imposed on a collaborative study will, due to
457 the inter-collaborator variation, be more difficult for a candidate BIM to achieve than would be a
458 performance requirement imposed on a single laboratory validation study with the same number
459 of total replicates. The performance requirements imposed on a single laboratory study and a
460 collaborative study should be logically and statistically consistent.

461
462 The study director could, for example, prepare batches of SITM and SSTM and then prepare
463 samples of mixtures at the 0%:100%, 33%:67%, 67%:33% and 100%:0% proportions. From
464 each of the well-mixed sample aliquots, test portions would be selected such that each
465 participating collaborator would receive the requisite number of replicates (see Section 9). All
466 test portions for each collaborator would be randomly assigned IDs before distribution. The
467 study is masked so that collaborators cannot visually identify the composition of the test
468 portions. Additional unmasked test portions may be provided for proficiency training purposes.

469
470 Each collaborator would use the BIM according to instructions to analyze each test portion
471 provided, and report results by test portion number and 1 = Identified or 0 = Not Identified.

472
473 Now suppose a collaborative study is to be evaluated with respect to the performance
474 requirements of Table 2. The primary goal is to validate that performance is sufficiently
475 homogeneous across collaborators and that the performance requirements are met. As
476 mentioned before, the number of replicate test portions for each collaborator should be 12 or
477 more to control the quantal repeatability error sufficiently to allow detection of an
478 intercollaborator effect. Suppose the plan was to enroll 12 collaborators with the expectation
479 that 1 or 2 might have to be removed for cause (spoilage of test portions, failing to follow
480 instructions, cross-contamination, etc.) Consequently 144 test portions are prepared for each of
481 the four % SSTM values (0, 33.3%, 66.7%, 100%).

482
483 After completion of the study, two collaborators were removed for cause, and the results shown
484 in Table 6 were obtained. For the 0 % SSTM concentration, the statistical analysis of the data
485 gives the results in Table 7. There is no detected intercollaborator effect (p-value = 0.43, point
486 estimate = 0.00, and the confidence interval includes 0.000 and has an upper limit of 0.040), and
487 the upper 2-sided confidence limit for combined POI is 0.0457, well below the performance
488 requirement of 0.10. There is little evidence the method is irreproducible, and the method meets
489 the POI (or FPF) performance requirement.

490
491 For the 33 % SSTM concentration, the statistical analysis of the data gives the results in Table 8.
492 Again, there is no detected intercollaborator effect (p-value = 0.66), so there is little evidence
493 that the method is irreproducible.

494
495 For the 67 % SSTM concentration, the statistical analysis of the data gives the results in Table 9.
496 Once again is no detected intercollaborator effect (p-value = 0.18), so there is little evidence the
497 method is irreproducible.

498
499 Finally, for the 100 % SSTM concentration, the statistical analysis of the data gives the results in
500 Table 10. There is no detected intercollaborator effect (p-value = 0.25, point estimate = 0.027,
501 and the confidence interval includes 0.000 and has an upper limit of 0.093), and the lower 2-

502 sided confidence limit for combined POI is 0.917, well above the performance requirement of
503 0.90. There is little evidence the method is irreproducible, and the method meets the POI (or
504 FNF) performance requirement.

505

506 **11. Lot-Lot Variability Study, Time Stability Study and Robustness Study**

507

508 The single laboratory and collaborative studies discussed above do not represent worst-case, end-
509 of-life conditions with respect to method materials and parameters. For this reason, it is
510 customary to augment these studies with additional studies to verify proper results despite
511 reasonable variations among method materials, equipment and parameters.

512

513 A “lot-lot variability” study is meant to verify results across different lots of method materials
514 (supplies used) and sets of equipment. Each lot would consist of a different manufactured or
515 prepared batch of materials (reagents, supplies, etc.) and possibly a different set of measurement
516 equipment. Date of manufacture is not an issue in this study, only variation among lots, so
517 ideally the lots tested should have been produced at near the same times. Just as with
518 collaborators in a collaborative study, estimation of the lot random effect requires at least 6
519 different lots be involved in the study. Each lot should result in attainment of any BIM
520 performance requirements, and the variation in performance among lots should be immaterial in
521 size.

522

523 A “time stability” study is meant to verify there is no material degradation in performance over
524 the life of lots of materials and equipment. This may be accomplished by determination of
525 parametric aging effect by use of time-staggered lots, or simply verifying performance on end-
526 of-life lots.

527

528 Note that the “lot-lot variability” and “time-stability” studies cannot be merged into a single
529 study unless there are sufficient replicate lots at or near the same time point(s) to allow
530 separation of the lot-lot and time effects. If lot-lot and time effects are negatively correlated, one
531 factor may mask the effect of the other in an inadequate combined study (e.g., a different single
532 lot at each different time point). Testing only end-of-life lots would be a satisfactory combined
533 study even though time and lot effects could not be resolved.

534

535 A “robustness” study (also denoted a “sensitivity” study) is meant to verify performance under
536 worst-case conditions of method critical parameter (e.g., times, temperatures, concentrations)
537 variation. Disturbances of method parameters should reflect maximum excursions to be
538 expected in practical use. Performance requirements should be met at each of these excursions.
539 The statistical design should be capable of measuring at least main effects.

540

541 **12. Conclusion**

542

543 The purpose of a qualitative BIM is to discriminate between acceptable target material and target
544 material with an unacceptable concentration of non-target material. This concept was
545 particularized to discrimination between the SSTM and SITM for the purpose of method
546 validation. A general overview of the application of the POI model and analysis has been given
547 which allows validation and/or characterization of qualitative BIMs. Examples have been given

548 for both single laboratory and collaborative studies with SMPRs. The use of POI statistics
549 harmonizes statistical concepts among botanical, microbiological, toxin and other analyte
550 identification or detection methods for which binary results are obtained. The POI statistical
551 model provides a tool for graphical representation of response curves for qualitative methods,
552 reporting of descriptive statistics, and application of performance requirements.
553

554 **13. Acknowledgements**

555

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557 kindly reviewing this article and supplying numerous comments for improvement. In particular,
558 we wish to thank Paul Wehling of Medallion Laboratories and Danica Reynaud of
559 AuthenTechnologies for the extraordinary amount of time they spent in both review and
560 providing constructive criticism.
561

562 **14. References**

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591 Table 1: *Panax* samples analyzed in this Study

592

593

| N | Label | Provider | Source |
|---|--|--|--------|
| Inclusivity Panel (American ginseng) | | | |
| 26 | American ginseng | Ginseng Board of Wisconsin | USA |
| 13 | American ginseng | American Herbal Pharmacopoeia | USA |
| 4 | American ginseng | Internet Retailer (Wisconsin farm) | USA |
| Exclusivity Panel (Chinese ginseng) | | | |
| 3 | Chinese ginseng, red | American Herbal Pharmacopoeia ² | China |
| 1 | Kirin Red #1 | Internet Retailer | China |
| 1 | Kirin Red #3 | Internet Retailer | China |
| 1 | Kirin Red #5 | Internet Retailer | China |
| 1 | Shih Chu #25 | Internet Retailer | China |
| 1 | Shih Chu #80 | Internet Retailer | China |
| SSTM* | | | |
| 344 | 0.98 American ginseng + 0.02 Chinese ginseng | | |
| SITM* | | | |
| 344 | 0.90 American ginseng + 0.10 Chinese ginseng | | |

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614 *In each case, each of the 43 American ginseng samples were mixed with each of the 8 Chinese

615 ginseng samples (43x8=344)

616

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619

| Requirement | % SSTM | Measure | Maximum | # Replicates to be tested | # Failures allowed |
|--------------------|---------------|-----------------|-----------------|----------------------------------|---------------------------|
| POI | 100% | 95% 1-sided LCL | 0.90 (FNF<0.10) | 60 | 2 |
| POI | 0% | 95% 1-sided UCL | 0.10 (FPF<0.10) | 60 | 2 |

NOTE: In each case, no more than 2 failures are allowed.

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623

Table 3. Alternative test plans to obtain 1-sided upper 95% modified Wilson confidence limit at or below specified maximum value for FNF or FPF.^a

| Specified maximum^b | # Replicates to be tested | # Failures allowed^c | 1-sided 95% UCL^d | 2-sided 95% LCL^e | 2-sided 95% UCL^e | AOQL^f |
|--------------------------------------|----------------------------------|---------------------------------------|------------------------------------|------------------------------------|------------------------------------|-------------------------|
| 0.20 | 11 | 0 | 0.197 | 0.000 | 0.259 | 0.129 |
| 0.20 | 20 | 1 | 0.196 | 0.000 | 0.236 | 0.118 |
| 0.20 | 24 | 1 | 0.167 | 0.000 | 0.202 | 0.101 |
| 0.20 | 36 | 3 | 0.191 | 0.029 | 0.218 | 0.124 |
| 0.20 | 48 | 5 | 0.199 | 0.045 | 0.222 | 0.133 |
| 0.20 | 72 | 8 | 0.187 | 0.057 | 0.204 | 0.131 |
| 0.15 | 20 | 0 | 0.119 | 0.000 | 0.161 | 0.081 |
| 0.15 | 24 | 0 | 0.101 | 0.000 | 0.138 | 0.069 |
| 0.15 | 36 | 1 | 0.115 | 0.000 | 0.142 | 0.071 |
| 0.15 | 48 | 3 | 0.146 | 0.021 | 0.168 | 0.095 |
| 0.15 | 72 | 5 | 0.136 | 0.030 | 0.152 | 0.091 |
| 0.10 | 40 | 0 | 0.063 | 0.000 | 0.088 | 0.044 |
| 0.10 | 48 | 1 | 0.088 | 0.000 | 0.109 | 0.054 |
| 0.10 | 60 | 2 | 0.096 | 0.009 | 0.114 | 0.061 |
| 0.10 | 72 | 3 | 0.100 | 0.014 | 0.115 | 0.065 |
| 0.05 | 60 | 0 | 0.043 | 0.000 | 0.060 | 0.030 |
| 0.05 | 72 | 0 | 0.036 | 0.000 | 0.051 | 0.025 |
| 0.05 | 96 | 1 | 0.045 | 0.000 | 0.057 | 0.028 |
| 0.02 | 130 | 0 | 0.020 | 0.000 | 0.029 | 0.014 |
| 0.02 | 240 | 1 | 0.018 | 0.000 | 0.023 | 0.012 |
| 0.01 | 280 | 0 | 0.010 | 0.000 | 0.014 | 0.007 |

^a Excerpted from LaBudde(7).

^b Desired maximum level of FNF or FPF to attain with 95% confidence.

^c Maximum number of failures that can occur in the replicates tested and still meet specification.

^d Worst-case 1-sided 95% modified Wilson upper confidence limit on FNF or FPF if maximum failures are observed.

^e 95% modified Wilson 2-sided confidence interval on FNF or FPF if maximum failures are observed.

^f Observed FNF or FPF corresponding to maximum failures allowed.

624

625

Table 4. Observed SLV Results for Example BIM

| % SSTM | # Test Portions | # Identified | # Not Identified | POI |
|---------------|------------------------|---------------------|-------------------------|------------|
| 0.0% | 60 | 1 | 59 | 0.0167 |
| 33.3% | 60 | 7 | 53 | 0.1167 |
| 66.7% | 60 | 27 | 33 | 0.4500 |
| 100.0% | 60 | 60 | 0 | 1.0000 |

626

627

Table 5. Reported SLV Results

| % SSTM | n | ID | not ID | POI | 1-sided 95% | LCL 95% | UCL 95% |
|---------------|----------|-----------|---------------|------------|--------------------|----------------|----------------|
| 0.0% | 60 | 1 | 59 | 0.0167 | 0.0713 | 0.0000 | 0.0886 |
| 33.3% | 60 | 7 | 53 | 0.1167 | | 0.0577 | 0.2218 |
| 66.7% | 60 | 27 | 33 | 0.4500 | | 0.3309 | 0.5751 |
| 100.0% | 60 | 60 | 0 | 1.0000 | 0.9568 | 0.9398 | 1.0000 |

628

629

630 Table 6: Collaborative study results.

| <i>% SSTM</i> | <i>Collaborator</i> | <i>Replicates</i> | <i># Identified</i> |
|---------------|---------------------|-------------------|---------------------|
| 0 | 1 | 12 | 1 |
| 0 | 2 | 12 | 0 |
| 0 | 3 | 12 | 0 |
| 0 | 4 | 12 | 0 |
| 0 | 5 | 12 | 0 |
| 0 | 6 | 12 | 0 |
| 0 | 7 | 12 | 0 |
| 0 | 8 | 12 | 0 |
| 0 | 9 | 12 | 0 |
| 0 | 10 | 12 | 0 |
| 33.33 | 1 | 12 | 2 |
| 33.33 | 2 | 12 | 2 |
| 33.33 | 3 | 12 | 2 |
| 33.33 | 4 | 12 | 2 |
| 33.33 | 5 | 12 | 0 |
| 33.33 | 6 | 12 | 1 |
| 33.33 | 7 | 12 | 1 |
| 33.33 | 8 | 12 | 4 |
| 33.33 | 9 | 12 | 2 |
| 33.33 | 10 | 12 | 3 |
| 66.67 | 1 | 12 | 4 |
| 66.67 | 2 | 12 | 9 |
| 66.67 | 3 | 12 | 5 |
| 66.67 | 4 | 12 | 8 |
| 66.67 | 5 | 12 | 7 |
| 66.67 | 6 | 12 | 4 |
| 66.67 | 7 | 12 | 7 |
| 66.67 | 8 | 12 | 3 |
| 66.67 | 9 | 12 | 8 |
| 66.67 | 10 | 12 | 5 |
| 100 | 1 | 12 | 12 |
| 100 | 2 | 12 | 10 |
| 100 | 3 | 12 | 11 |
| 100 | 4 | 12 | 12 |
| 100 | 5 | 12 | 12 |
| 100 | 6 | 12 | 11 |
| 100 | 7 | 12 | 12 |
| 100 | 8 | 12 | 12 |
| 100 | 9 | 12 | 12 |
| 100 | 10 | 12 | 12 |

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634 Table 7: Collaborative study results for 0 % SSTM concentration.
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AOAC Binary Data Interlaboratory Study Workbook

Version: 2.2

Study Reported Values

| Seq. | Item | Symbol | Value | Approx. 95% LCL | Approx. 95% UCL |
|------|--|--------------|----------|-----------------------|-----------------------|
| | Sample ID: | | 0 % SSTM | | |
| | 1 Total number of laboratories | p | 10 | | |
| | 2 Total number of replicates | Sum(n(L)) | 120 | | |
| | 3 Overall mean of all data (grand mean) | LPOI or LPOD | 0.0083 | 0.0015 | 0.0457 |
| | 4 Repeatability standard deviation | s(r) | 0.0913 | 0.0807 | 0.1713 |
| | 5 Among-Laboratories standard deviation | s(L) | 0.0000 | 0.0000 | 0.0402 |
| | 6 Homogeneity test of laboratory PODs | p-value | 0.4303 | | |
| | 7 Reproducibility standard deviation | s(R) | 0.0913 | 0.0814 | 0.1064 |
| | 8 Intraclass correlation coefficient for repeatability | l(r) | 1.0000 | 0.8335 | 1.0000 |

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Table 8. Collaborative study results for 33.33 % SSTM concentration.

AOAC Binary Data Interlaboratory Study Workbook

Version: 2.2

Study Reported Values

| Seq. | Item | Symbol | Value | Approx. 95% LCL | Approx. 95% UCL |
|------|--|--------------|--------------|-----------------------|-----------------------|
| | Sample ID: | | 33.33 % SSTM | | |
| | 1 Total number of laboratories | p | 10 | | |
| | 2 Total number of replicates | Sum(n(L)) | 120 | | |
| | 3 Overall mean of all data (grand mean) | LPOI or LPOD | 0.1583 | 0.0913 | 0.2253 |
| | 4 Repeatability standard deviation | s(r) | 0.3703 | 0.3272 | 0.4266 |
| | 5 Among-Laboratories standard deviation | s(L) | 0.0000 | 0.0000 | 0.1400 |
| | 6 Homogeneity test of laboratory PODs | p-value | 0.6563 | | |
| | 7 Reproducibility standard deviation | s(R) | 0.3703 | 0.3304 | 0.4275 |
| | 8 Intraclass correlation coefficient for repeatability | l(r) | 1.0000 | 0.8889 | 1.0000 |

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647 Table 9: Collaborative study results for 66.67 % SSTM concentration.
 648

AOAC Binary Data Interlaboratory Study Workbook

Version: 2.2

Study Reported Values

| Seq. | Item | Symbol | Value | Approx. 95% LCL | Approx. 95% UCL |
|------|--|--------------|--------------|-----------------------|-----------------------|
| | Sample ID: | | 66.67 % SSTM | | |
| | 1 Total number of laboratories | p | 10 | | |
| | 2 Total number of replicates | Sum(n(L)) | 120 | | |
| | 3 Overall mean of all data (grand mean) | LPOI or LPOD | 0.5000 | 0.3919 | 0.6081 |
| | 4 Repeatability standard deviation | s(r) | 0.4939 | 0.4364 | 0.5222 |
| | 5 Among-Laboratories standard deviation | s(L) | 0.0948 | 0.0000 | 0.2779 |
| | 6 Homogeneity test of laboratory PODs | p-value | 0.1783 | | |
| | 7 Reproducibility standard deviation | s(R) | 0.5029 | 0.4489 | 0.5222 |
| | 8 Intraclass correlation coefficient for repeatability | l(r) | 0.9644 | 0.7547 | 1.0000 |

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Table 10: Collaborative study results for 100.0 % SSTM concentration.

AOAC Binary Data Interlaboratory Study Workbook

Version: 2.2

Study Reported Values

| Seq. | Item | Symbol | Value | Approx. 95% LCL | Approx. 95% UCL |
|------|--|--------------|--------------|-----------------------|-----------------------|
| | Sample ID: | | 100.0 % SSTM | | |
| | 1 Total number of laboratories | p | 10 | | |
| | 2 Total number of replicates | Sum(n(L)) | 120 | | |
| | 3 Overall mean of all data (grand mean) | LPOI or LPOD | 0.9667 | 0.9174 | 0.9870 |
| | 4 Repeatability standard deviation | s(r) | 0.1784 | 0.1576 | 0.2055 |
| | 5 Among-Laboratories standard deviation | s(L) | 0.0273 | 0.0000 | 0.0930 |
| | 6 Homogeneity test of laboratory PODs | p-value | 0.2506 | | |
| | 7 Reproducibility standard deviation | s(R) | 0.1804 | 0.1610 | 0.2121 |
| | 8 Intraclass correlation coefficient for repeatability | l(r) | 0.9772 | 0.7818 | 1.0000 |

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Figure Captions

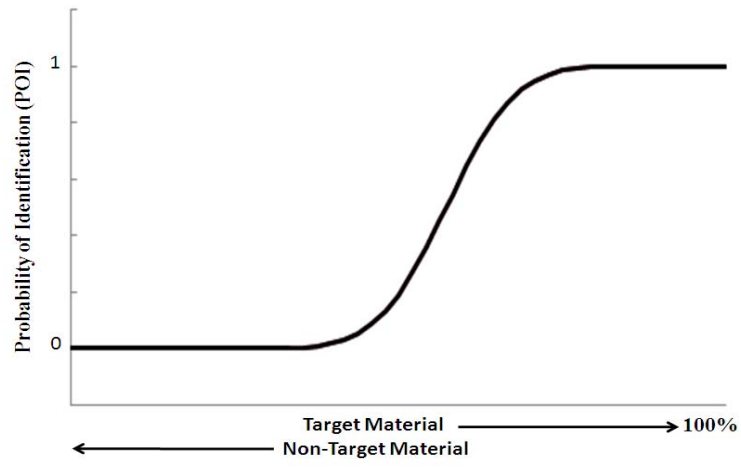
- 659
660
661 Figure 1 Probability of Identification for botanical identification.
662
663 Figure 2 Inclusivity/exclusivity and SSTM/SITM characterization.
664
665 Figure 3 Conversion of SSTM, SITM, and intermediate concentrations to POI.
666
667 Figure 4 SIMCA plots for A) 100% American ginseng and 100% Chinese ginseng, B) SSTM,
668 100% American ginseng, and 100% Chinese ginseng, and C) SITM, 100% American
669 ginseng, and 100% Chinese ginseng. Legend: **Red** – American ginseng (AG),
670 **Green** – Chinese ginseng (CG), and **Blue** – B) SSTM and C) SITM.
671
672 Figure 5 Target material American ginseng, non-target material Chinese ginseng: A) SITM
673 and SSTM and B) POI.
674
675 Figure 6 Expected POI vs. % SSTM for an example BIM. Note the POI at 0% is the false
676 positive fraction. 1- POI at 100% is the false negative fraction.
677
678

679 Figure 1: Probability of Identification for botanical identification

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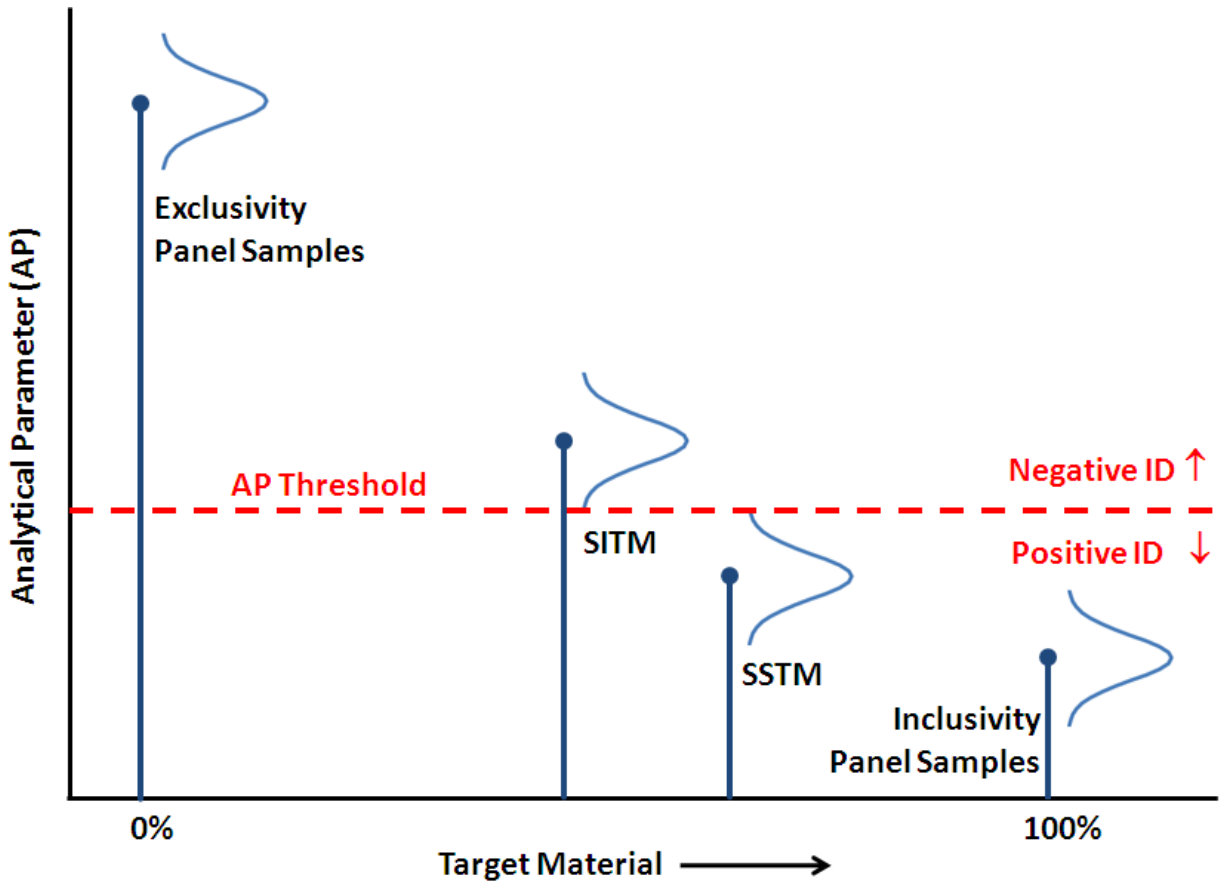
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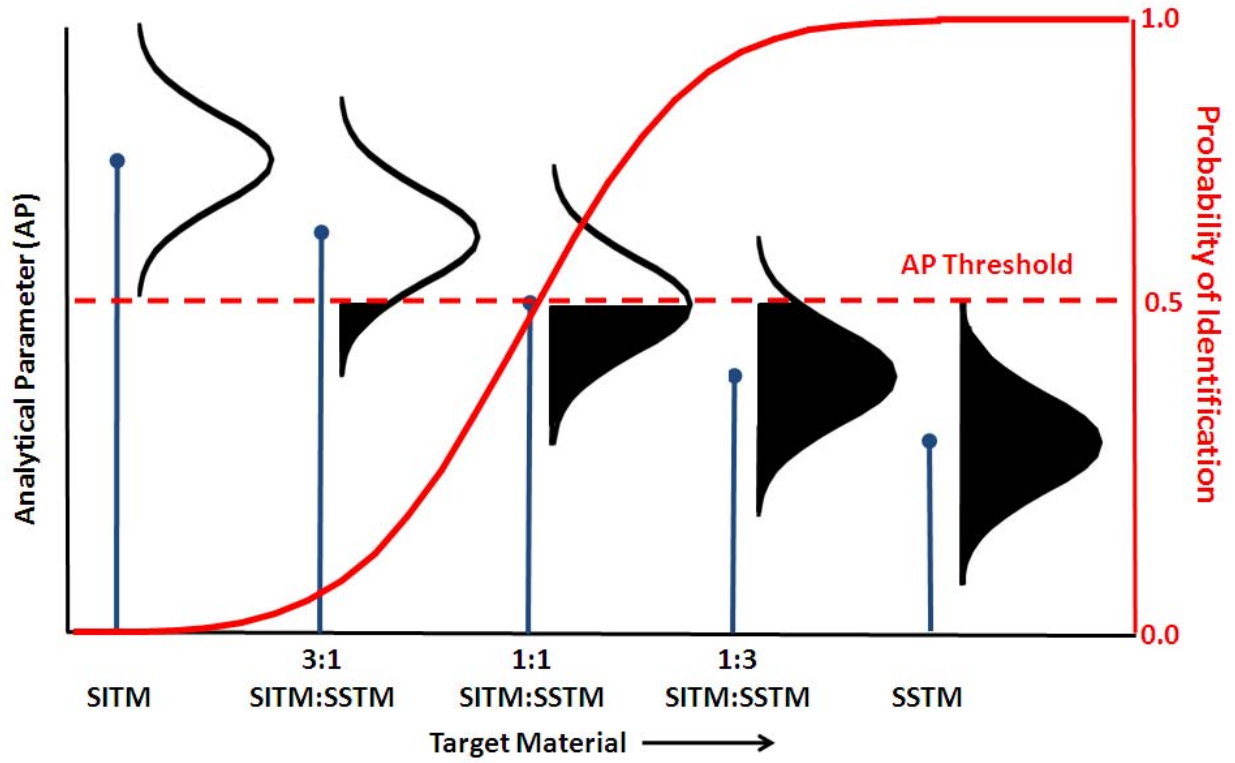
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686 Figure 2: Inclusivity/exclusivity and SSTM/SITM characterization.
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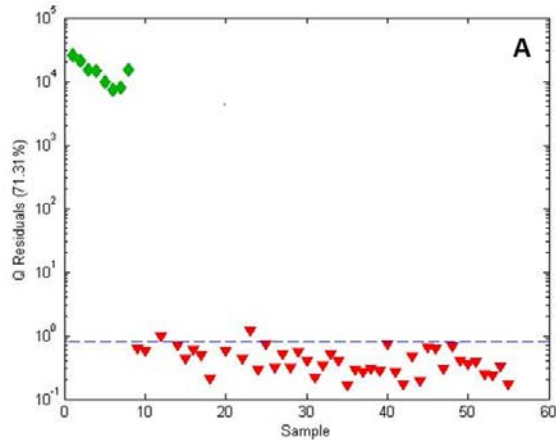
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691 Figure 3: Conversion of SSTM, SITM, and intermediate concentrations to POI.
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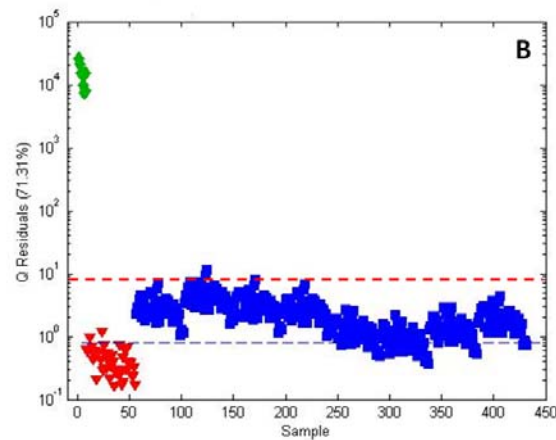


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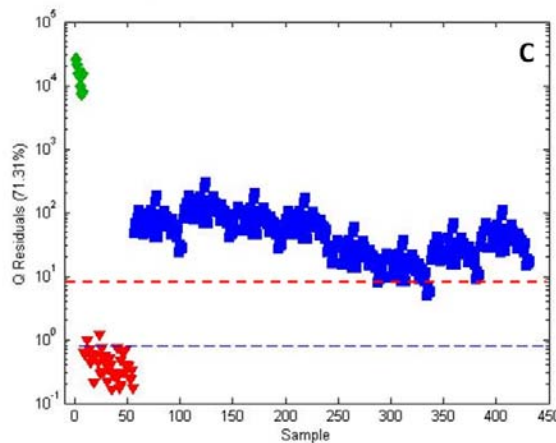
696 Figure 4: SIMCA plots for A) 100% American ginseng and 100% Chinese ginseng, B) SSTM,
697 100% American ginseng, and 100% Chinese ginseng, and C) SITM, 100% American ginseng,
698 and 100% Chinese ginseng. Legend: **Red** – American ginseng (AG), **Green** – Chinese ginseng
699 (CG), and **Blue** – B) SSTM and C) SITM.
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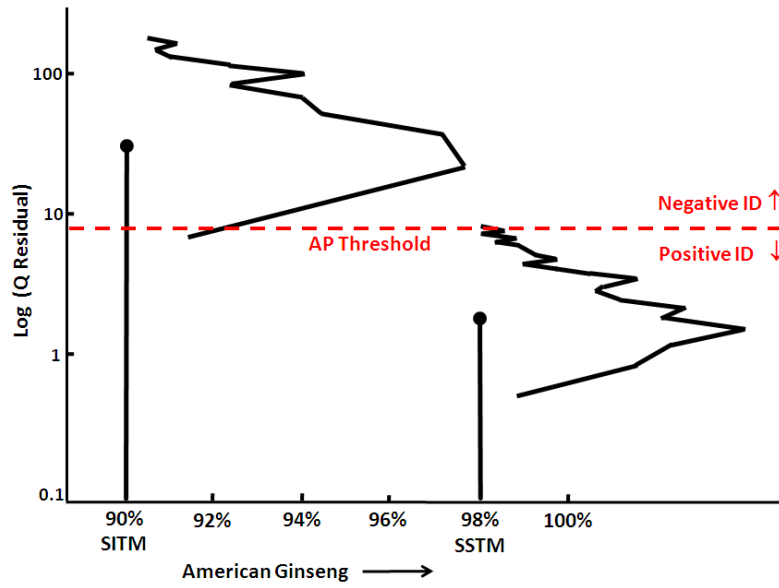


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708 Figure 5: Target material American ginseng, non-target material Chinese ginseng: A) SITM and
709 SSTM and B) POI.

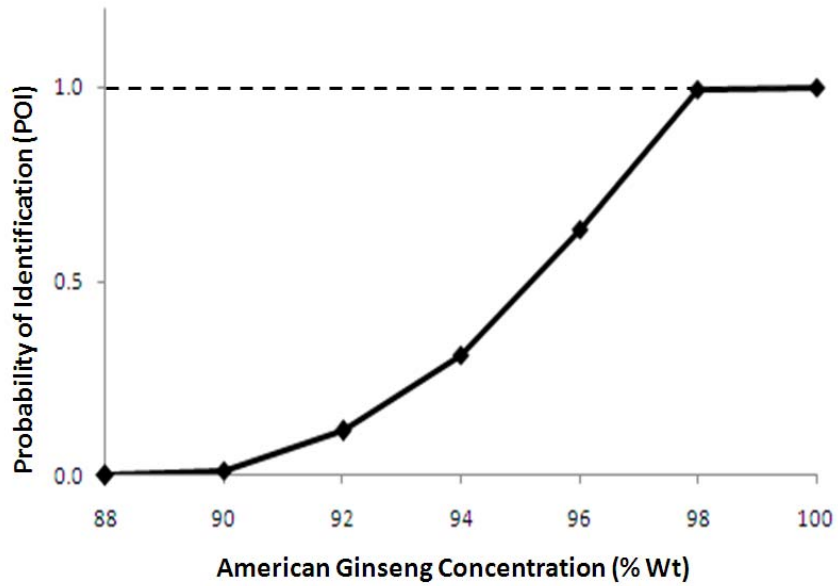
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711 **A**



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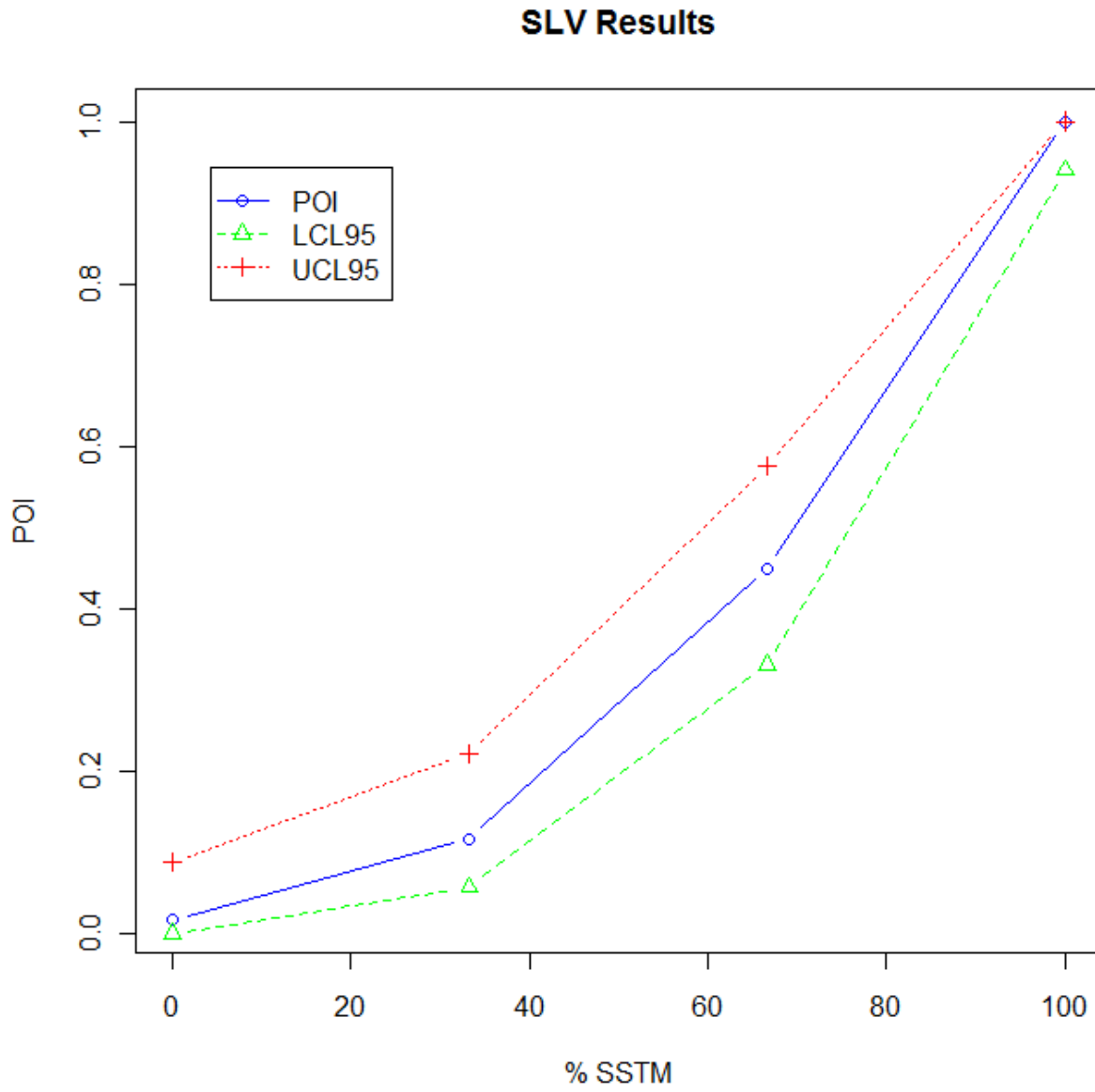
714 **B**



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Figure 6: Expected POI vs. % SSTM for an example BIM. Note the POI at 0% is the false positive fraction. 1- POI at 100% is the false negative fraction.



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719

720 **Appendix A: SIMCA**

721
722 Principal component analysis (PCA) is a mathematical procedure that is used to convert
723 observations for samples with a large number of possibly correlated variables (ions, wavelength,
724 or wavenumbers) into a set of uncorrelated variables called principal components (A1). The
725 transformation takes place in manner that assigns the maximum variance to the first principal
726 component with less variance being accounted for by each successive principal component.
727 PCA is applied to the entire data set to determine what groupings of the samples can be seen
728 without any prior decisions (i.e., it is unsupervised). The first 2 or 3 principal components
729 (displayed as 2 or 3 dimensional plots) can be used to demonstrate general patterns in the data.
730

731 SIMCA (soft independent modeling of class analogy) is a supervised approach that builds a PCA
732 model for each specified category of samples (A2). Distances between the models are then used
733 to determine the independence of each category of samples. New samples can be assigned to
734 one of the categories or classified as not fitting in any of them.
735

736 SIMCA is used for BIMs because predetermined categories of samples are established and
737 modeled. For a BIM, however, only a single PCA model is constructed and that is for the
738 samples in the inclusivity panel. All other samples are then evaluated using the PCA model to
739 determine whether it is described by the inclusivity PCA model or whether it lies a significant
740 distance from the model, i.e., it doesn't belong to the inclusivity panel category of samples.
741

742 Two statistics that are used to evaluate whether a sample fits the PCA model are the Q residual
743 and the Hotelling T^2 statistic. The Hotelling T^2 statistic is the multivariate analog of the
744 univariate Students' t statistic. It describes how a sample fits in the model. The Q residual, also
745 called the squared prediction error (SPE), is more commonly used for process control
746 applications. It describes how far a sample falls outside the model. Some chemometric
747 programs provide both of these statistics as a means of evaluating the fit of a PCA model to the
748 data (1).
749

750 Figure A1 provides a simplified illustration of the relationship of the two statistics. In this case,
751 a PCA model is fit to one category of samples (black dots). Since only the first principal
752 component was used for this model, the model is a straight line. The data have been mean
753 centered, so they are centered around the origin, i.e. the intersection of the x and y axis. The
754 distribution of each sample with respect to the model is determined by dropping a line from the
755 sample point perpendicular to the model line. The distance from the point where the
756 perpendicular of a sample intersects the model line to the origin provides the Hotelling T^2 value
757 for that point. With sufficient data and a normal distribution, the data distribution should appear
758 as a bell-shaped function centered at the origin. Using this distribution, it can be determined
759 whether a sample is well-fit by the model, i.e. falls inside the 95% confidence limits.
760

761 The variance of the sample data with respect to the model is the variance computed along the
762 straight line. In this case it would be analogous the Students' t calculation, i.e. the sum of square
763 of the distance for each sample. In Figure A1, the first principal component for the modeled
764 category (black dots) passes through the sample data in a manner that provides the maximum
765 variance. A second principal component, perpendicular to the first, would account for the

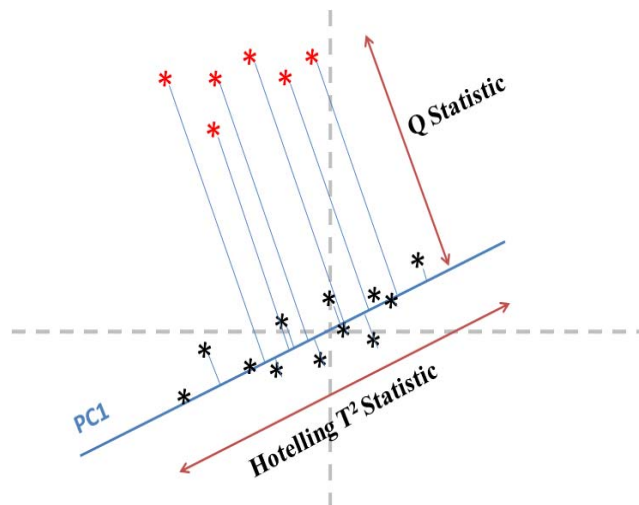
766 distance of the points from the line and, in this case, provide far less variance than the first
767 principal component. For a model based just on the first principal component, the variance
768 associated with the distance of the sample points from the line is accounted for by the Q residual.
769

770 The distribution of un-modeled data from a second category of samples (the red dots) can be
771 evaluated using the model for the first category of samples. As shown in Figure A1, the
772 distribution of the second category of samples on the first model is very reasonable.
773 Perpendicular lines from the samples in the second category intercept the model line at
774 reasonable distances from the origin. If this were real data, and a 95% confidence limit had been
775 computed, the second category of samples would undoubtedly be within that limit. However, for
776 the second category of samples, a much larger fraction of the total variance is incorporated in the
777 distance from the model line. The second category samples will fall well outside the 95%
778 confidence limit for the Q residual established by the first category samples.
779

780 SIMCA can be applied to a BIM by constructing a PCA model using the data from the
781 inclusivity panel botanical materials. New samples are fit to the model and the Q residual is
782 determined. the Q residual for a sample falls outside the 95% confidence limit, the new sample
783 is not the same as the target materials. Conversely, if the new sample falls within the 95%
784 confidence limit, it would be classified as a target material.
785

786 Figure A1: Illustration of Hotelling T2 and Q statistic: *) modeled samples and *) unknown
787 samples.
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792 References:

793

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798

799

A2 Wold, S. (1987) Principal component analysis. *Chemom. Intel. Sys.* 2, 37-52.

800

801 Appendix B: Modeling of the POI Using Logistic Regression

802
803 The models in common use for this kind of problem include, among many others: 1)
804 discriminant analysis; 2) logistic regression; or 3) normit regression. There is also a choice of
805 metamer x (i.e., transform of %SSTM). Common choices include $x = \% \text{ SSTM}$, or $x =$
806 $\log_{10}(\% \text{ SSTM} + 0.5)$. Logistic and normit regression assume the POI vs. x curve is symmetric,
807 which that of Fig. 4 obviously is not.

808
809 Suppose we choose logistic regression with an identity metamer ($x = \% \text{ SSTM}$), which implies
810 the model

$$811 \text{logit(POI)} = \ln\{\text{POI} / (1 - \text{POI})\} = \alpha + \beta x = \alpha + \beta (\% \text{ SSTM}) \quad (\text{C.1})$$

812
813
814 For the sample data, the fit is:

```
815 Call:
816 glm(formula = cbind(id, notid) ~ x, family = binomial("logit"),
817     data = dat)
818
819 Deviance Residuals:
820     1       2       3       4
821  0.8314  0.9386 -1.5687  2.6222
822
823 Coefficients:
824             Estimate Std. Error z value Pr(>|z|)
825 (Intercept) -5.04711    0.67021  -7.531 5.05e-14 ***
826 x             0.07878    0.01001   7.869 3.57e-15 ***
827 ---
828 Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
829
830 (Dispersion parameter for binomial family taken to be 1)
831
832     Null deviance: 186.241  on 3  degrees of freedom
833 Residual deviance:  10.908  on 2  degrees of freedom
834 AIC: 25.12
835
836 Number of Fisher Scoring iterations: 5
```

837
838
839 The model fits poorly and is highly overdispersed (dispersion = $10.908 / 2 = 5.454$).
840 Consequently the standard errors found in the fit should be multiplied by $2.34 = \sqrt{5.454}$. (Note
841 that this overdispersion suggests that the logistic regression model with specified link is a poor
842 choice for these data.)

843
844 An estimate of the point at which $\text{POI} = 0.5000$ is given by the negative ratio of the intercept by
845 the slope, or $x = 64.1\% \text{ SSTM}$. This would be denoted “Effective Concentration at $\text{POI} = 0.50$ ”
846 or “EC50”. (It should be noted that EC50 depends upon the definitions of the SSTM and SITM.)

847
848 From the logistic regression fit, we get the results shown in Table B1 and Figure B1. The
849 logistic regression does not do as well as the direct POI descriptive statistics of Table 6, because
850 of serious failure of the model assumptions. (It turns out that *none* of the usual generalized model
851 forms fits the asymmetric POI vs. % SSTM curve very well for this example. So it should be
852 noted that the standard error of POI is *not* always reduced by fitting across the combination of
853 concentrations used.) Note that, based on the logistic model, the BIM continues to pass the 0%
854 SSTM performance requirement, but fails the 100% SSTM requirement.

855
 856
 857
 858
 859
 860

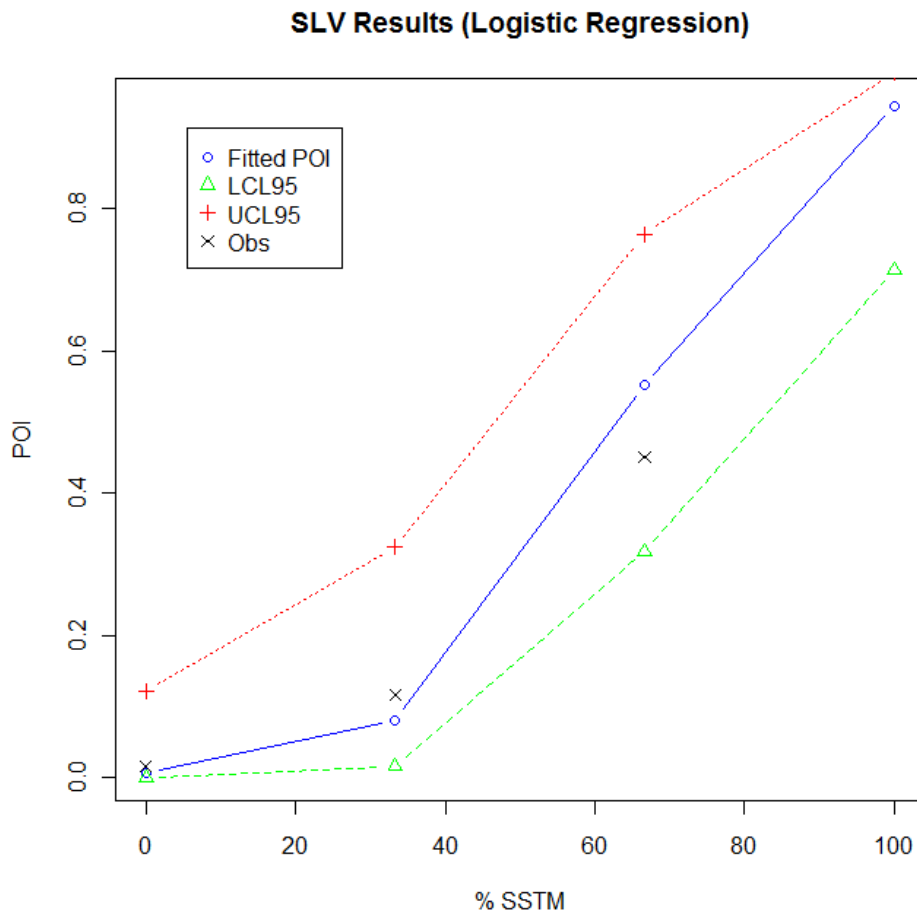
It is generally recommended that the methods of Table 6 be used for evaluating performance requirements, rather than those of unvalidated regression models. One of the advantages, however, of fitting such a model is that continuous curves may be obtained as shown in Figure B2.

Table B1. SLV Results (Logistic Regression Fit)

| % SSTM | Fitted POI | Obs. POI | 1-sided 95% | LCL 95% | UCL 95% |
|---------------|-------------------|-----------------|--------------------|----------------|----------------|
| 0.0% | 0.0064 | 0.0167 | 0.0778 | 0.0003 | 0.1214 |
| 33.3% | 0.0816 | 0.1167 | | 0.0162 | 0.3239 |
| 66.7% | 0.5511 | 0.4500 | | 0.3181 | 0.7636 |
| 100.0% | 0.9443 | 1.0000 | 0.7715 | 0.7126 | 0.9915 |

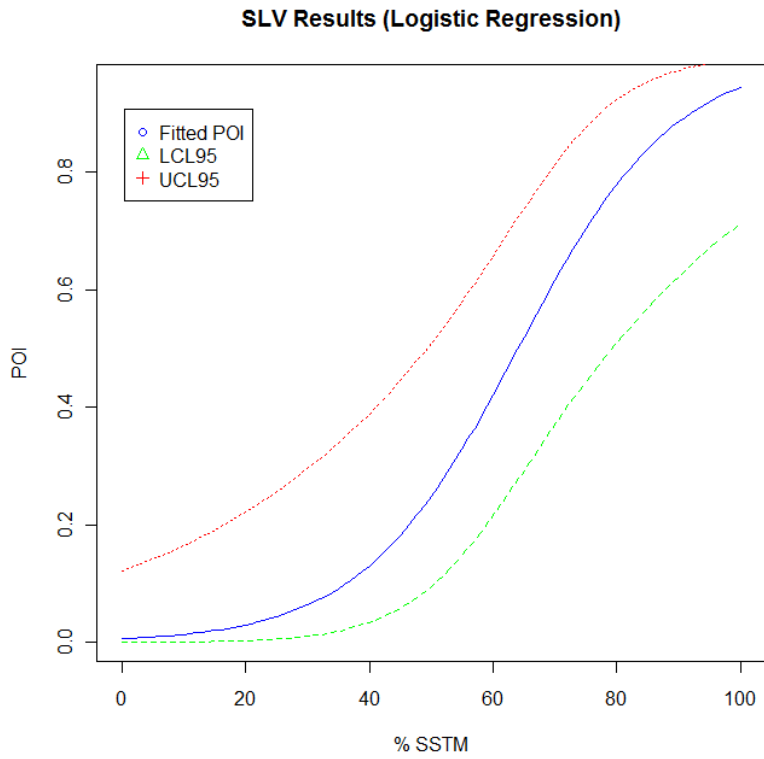
861
 862

863 Figure B1: Example SLV results from a logistic regression fit.



864
 865

866 Figure B2: Continuous curves from SLV logistic regression fit.



867